# Package 'famTEMsel' 

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## Type Package

Title Functional Additive Models for Treatment Effect-Modifier Selection

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Description
An implementation of a functional additive regression model which is uniquely modified and constrained to model nonlinear interaction effects between a categorical treatment variable and a potentially large number of functional/scalar pretreatment covariates on their effects on a scalarvalued outcome. The model generalizes functional additive models by incorporating treatmentspecific components into additive effect components, however, a structural constraint is imposed on the treatment-specific components, to give a class of orthogonal main and interaction effect additive models. If primary interest is in interactions, one can avoid estimating main effects, obviating the need to specify their form and thereby avoiding the issue of model misspecification. Utilizing this orthogonality, one can effectively conduct treatment effect-modifier variable selection. The selected covariates can be used to make individualized treatment recommendations. We refer to Park, Petkova, Tarpey, and Ogden (2020) [doi:10.1016/j.jspi.2019.05.008](doi:10.1016/j.jspi.2019.05.008) and Park, Petkova, Tarpey, and Ogden (2020) "'Constrained functional additive models for estimating interactions between a treatment and functional covariates" (pre-print) for detail of the method. The main function of this package is famTEMsel().
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cv.famTEMsel

Functional Additive Models for Treatment Effect-Modifier Selection
(cross-validation function)

## Description

Does k-fold cross-validation for famTEMsel, selects an optimal regularization parameter index, lambda.opt.index, and returns the estimated constrained functional additive model given the optimal regularization parameter index lambda. opt. index.

## Usage

cv.famTEMsel(y, A, X, Z = NULL, mu.hat = NULL, n.folds = 5, d = 3, k = 6, bs = "ps", sp = NULL, lambda.opt.index = NULL, lambda $=$ NULL, nlambda $=30$, lambda.min.ratio $=0.01$, lambda.index.grid = 1:floor(nlambda/3), cv1sd = FALSE, thol $=1 \mathrm{e}-05$, max.ite $=1 \mathrm{e}+05$, regfunc $=$ "L1", max.iter $=10$, eps.iter = 0.01, eps.num.deriv = 1e-04, trace.iter = TRUE, plots = TRUE)

## Arguments

$y \quad$ a n-by-1 vector of responses
A a n-by-1 vector of treatment variable; each element represents one of the $\mathrm{L}(>1)$ treatment conditions; e.g., c( $1,2,1,1,3 \ldots$...); can be a factor-valued
$X \quad$ a length-p list of functional-valued covariates, with its jth element corresponding to a n-by-n.eval[j] matrix of the observed jth functional covariates; n.eval[j] represents the number of evaluation points of the jth functional covariates
Z a n-by-q matrix of scalar-valued covaraites
mu.hat a n-by-1 vector of the fitted (X,Z)-main effect term of the model provided by the user; defult is NULL, in which case mu. hat is taken to be a vector of zeros; the optimal choice for this vector is $\mathrm{E}(\mathrm{y} \mid \mathrm{X}, \mathrm{Z})$
n .folds number of folds for cross-validation; the default is 5 .
d
k
bs
sp
lambda.opt.index
a user-supplied optimal regularization parameter index to be used; the default is NULL, in which case n.folds cross-validation is performed to select an optimal index.
lambda a user-supplied regularization parameter sequence; typical usage is to have the program compute its own lambda sequence based on nlambda and lambda.min.ratio
nlambda total number of lambda values; the default value is 30 .
lambda.min.ratio
the smallest value for lambda, as a fraction of lambda.max, the (data derived) entry value (i.e. the smallest value for which all coefficients are zero); the default is $1 \mathrm{e}-2$.
lambda.index.grid
a set of indices of lambda, in which the search for an optimal regularization parameter is to be conducted.
cv1sd if TRUE, an optimal regularization parameter is chosen based on: the mean crossvalidated error +1 SD of the mean cross-validated error, which typically results in an increase in regularization; the defualt is FALSE.
thol stopping precision for the coordinate-descent algorithm; the default value is $1 \mathrm{e}-$ 5.
max.ite number of maximum iterations for the coordinate-descent procedure used in estimating the component functions; the default value is $1 \mathrm{e}+5$.
regfunc type of the regularizer for variable selection; the default is "L1"; can also be "MCP" or "SCAD".
max.iter number of maximum iterations for the iterative procedure used in estimating the single-index coefficient functions; the default value is $1 \mathrm{e}+1$.
eps.iter a value specifying the convergence criterion for the iterative procedure used in estimating the single-index coefficient functions; the defult is $1 \mathrm{e}-2$.
eps.num.deriv a small value that defines a finite difference used in computing the numerical (1st) derivative of the estimated component function; the default is $1 \mathrm{e}-4$.
trace.iter if TRUE, trace the estimation process by printing the difference in the estimated single-index basis coefficients (as compared to the previous iteration), and the functional norms of the estimated component functions, for each iteration.
plots if TRUE, produce a cross-validation plot of the estimated mean squared error versus the regulariation parameter index.

## Value

a list of information of the fitted constrained functional additive model including
famTEMsel.obj an object of class famTEMsel, which contains the sequence of the set of fitted component functions samTEMsel.obj implied by the sequence of the regularization parameters lambda and the corresponding set of fitted single-index coefficient functions si.fit; see famTEMsel for detail.
lambda.opt.index
an index number, indicating the index of the estimated optimal regularization parameter in lambda.
nonzero.index a set of numbers, indicating the indices of estimated nonzero component functions, evalated at the regularization parameter index lambda.opt.index.
nonzero.X.index
a set of numbers, indicating the indices of estimated nonzero component functions associated with the $p$ functional covariates, evalated at the regularization parameter index lambda.opt.index.
func_norm.opt ap-by-1 vector, indicating the norms of the estimated component functions evaluatd at the regularization parameter index lambda.opt.index, with each element corresponding to the norm of each estimated component function.
$c v . s t o r a g e \quad a$ n.folds-by-nlambda matrix of the estimated mean squared errors, with each column corresponding to each of the regularization parameters in lambda and each row corresponding to each of the n.folds folds.
mean.cv a nlambda-by-1 vector of the estimated mean squared errors, with each element corresponding to each of the regularization parameters in lambda.
sd.cv a nlambda-by-1 vector of the standard deviation of the estimated mean squared errors, with each element corresponding to each of the regularization parameters in lambda.

## Author(s)

Park, Petkova, Tarpey, Ogden

## See Also

famTEMsel, predict_famTEMsel, plot_famTEMsel

## Examples

```
p = q = 10 # p and q are the numbers of functional and scalar pretreatment covariates, respectively
n.train = 300 # training set sample size
n.test = 1000 # testing set sample size
n = n.train + n.test
# generate p pretreatment functional covariates X by first seting up functional basis:
n.eval = 50; s = seq(0, 1, length.out = n.eval) # a grid of support points
b1 = sqrt(2)*sin(2*pi*s)
b2 = sqrt(2)*cos(2*pi*s)
b3 = sqrt(2)*sin(4*pi*s)
b4 = sqrt(2)*cos(4*pi*s)
B = cbind(b1, b2, b3, b4) # a (n.eval-by-4) basis matrix
# randomly generate basis coefficients, and then add measurement noise
```

```
X = vector("list", length= p); for(j in 1:p){
    X[[j]] = matrix(rnorm(n*4, 0, 1), n, 4) %*% t(B) +
        matrix(rnorm(n*n.eval, 0, 0.25), n, n.eval) # measurement noise
}
Z = matrix(rnorm(n*q, 0, 1), n, q) # q scalar covariates
A = rbinom(n, 1, 0.5) + 1 # treatment variable taking a value in {1,2} with equal prob.
# X main effect on y; depends on the first 5 covariates
# the effect is generated randomly; randomly generated basis coefficients, scaled to unit L2 norm.
tmp = apply(matrix(rnorm(4*5), 4,5), 2, function(s) s/sqrt(sum(s^2) ))
main.effect = rep(0, n); for(j in 1:5){
    main.effect = main.effect + cos(X[[j]]%*% B %*%tmp[,j]/n.eval) # nonlinear effect (cosine)
}; rm(tmp)
# Z main effect on y; also depends on first 5 covariates
for(k in 1:5){
    main.effect = main.effect + cos(Z[,k])
}
# define (interaction effect) coefficient functions associted with X[[1]] and X[[2]]
beta1 = B %*% c(0.5,0.5,0.5,0.5)
beta2 = B %*% c(0.5,-0.5,0.5,-0.5)
# A-by-X ineraction effect on y; depends only on X[[1]] and X[[2]].
interaction.effect = (A-1.5)*( 2*sin(X[[1]]%*%beta1/n.eval) + 2*sin(X[[2]]%*%beta2/n.eval))
# A-by-Z ineraction effect on y; depends only on Z[,1] and Z[,2].
interaction.effect = interaction.effect + (A-1.5)*(Z[,1] + 2*sin(Z[,2]))
# generate outcome y
noise = rnorm(n, 0, 0.5)
y = main.effect + interaction.effect + noise
var.main <- var(main.effect)
var.interaction <- var(interaction.effect)
var.noise <- var(noise)
SNR <- var.interaction/ (var.main + var.noise)
SNR # "signal-to-noise" ratio
# train/test set splitting
train.index = 1:n.train
y.train = y[train.index]
X.train= X.test = vector("list", p); for(j in 1:p){
X.train[[j]] = X[[j]][train.index,]
X.test[[j]] = X[[j]][-train.index,]
}
A.train = A[train.index]
A.test = A[-train.index]
y.train = y[train.index]
y.test = y[-train.index]
Z.train = Z[train.index,]
Z.test = Z[-train.index,]
```

\# obtain an optimal regularization parameter and the corresponding model by running cv.famTEMsel(). cv.obj = cv.famTEMsel(y.train, A.train, X.train, Z.train)
lambda.opt.index = cv.obj\$lambda.opt.index \# optimal regularization parameter index cv.obj\$func_norm.opt \# L2 norm of the component functions, associated with lambda.opt.index. famTEMsel.obj = cv.obj\$famTEMsel.obj \# extract the fitted model associted with lambda.opt.index.

```
# see also, famTEMsel() for the detail of famTEMsel.obj.
famTEMsel.obj$nonzero.index # set of indices for the component functions estimated as nonzero
# plot the component functions estimated as nonzero
plot_famTEMsel(famTEMsel.obj, which.index = famTEMsel.obj$nonzero.index)
# make ITRs for subjects with pretreatment characteristics, X.test and Z.test
trt.rule = make_ITR_famTEMsel(famTEMsel.obj, newX = X.test, newZ = Z.test)$trt.rule
head(trt.rule)
# an (IPWE) estimate of the "value" of this particualr treatment rule, trt.rule:
mean(y.test[A.test==trt.rule])
# compare the above value to the following estimated "values" of "naive" treatment rules:
mean(y.test[A.test==1]) # a rule that assigns everyone to A=1
mean(y.test[A.test==2]) # a rule that assigns everyone to A=2
```

famTEMsel $\quad$| Functional Additive Models for Treatment Effect-Modifier Selection |
| :--- |
| (main function) |

## Description

The function famTEMsel implements estimation of a constrained functional additve model.

## Usage

```
famTEMsel(y, A, X, Z = NULL, mu.hat = NULL, d = 3, k = 6,
    bs = "ps", sp = NULL, lambda = NULL, nlambda = 30,
    lambda.min.ratio = 0.01, lambda.index = floor(nlambda/3),
    thol = 1e-05, max.ite = 1e+05, regfunc = "L1", eps.iter = 0.01,
    max.iter = 10, eps.num.deriv = 1e-04, trace.iter = TRUE)
```


## Arguments

y
A a n-by-1 vector of treatment variable; each element represents one of the $\mathrm{L}(>1)$ treatment conditions; e.g., $\mathrm{c}(1,2,1,1,3 \ldots)$; can be a factor-valued
$X \quad$ a length-p list of functional-valued covariates, with its jth element corresponding to a n-by-n.eval[j] matrix of the observed jth functional covariates; n.eval[j] represents the number of evaluation points of the jth functional covariates
Z a n-by-q matrix of scalar-valued covaraites
mu.hat a n-by-1 vector of the fitted (X,Z)-main effect term of the model provided by the user; defult is NULL, in which case mu. hat is taken to be a vector of zeros; the optimal choice for this vector is $\mathrm{E}(\mathrm{y} \mid \mathrm{X}, \mathrm{Z})$
d
k
number of basis spline functions to be used for each component function; the default value is $3 ; \mathrm{d}=1$ corresponds to the linear model number of basis spline functions to be used for each single-index coefficient function associated with each functional covariate;
$\left.\begin{array}{ll}\text { bs } & \begin{array}{l}\text { type of basis for representing the single-index coefficient functions; the defult } \\ \text { is "ps" (p-splines); any basis supported by mgcv::gam can be used, e.g., "cr" } \\ \text { (cubic regression splines) }\end{array} \\ \text { smoothing parameter associated with the single-index coefficient function; the } \\ \text { default is NULL, in which case the smoothing parameter is estimated based on } \\ \text { generalized cross-validation } \\ \text { a user-supplied regularization parameter sequence; typical usage is to have the } \\ \text { program compute its own lambda sequence based on nlambda and lambda.min.ratio. } \\ \text { total number of lambda values; the default value is } 30 \text {. }\end{array}\right]$

## Details

A constrained functional model represents the joint effects of treatment, pretreatment p functional covariates and q scalar covariates on an outcome variable via a sum of treatment-specific additive flexible component functions defined over the ( $p+q$ ) covariates, subject to the constraint that the expected value of the outcome given the covariates equals zero, while leaving the main effects of the covariates unspecified. The p pretreatment functional covariates appear in the model as 1dimensional projections, via inner products with corresponding single-index coefficient functions. Under this model, the treatment-by-covariates interaction effects are determined by distinct shapes (across treatment levels) of the treatment-specific flexible component functions. Optimized under a penalized least square criterion with a L1 (or SCAD/MCP) penalty, the constrained functional additive model can effectively identify/select treatment effect-modifiers (from the p functional and q scalar covariates) that exhibit possibly nonlinear interactions with the treatment variable; this is achieved by producing a sparse set of estimated component functions of the model. The estimated nonzero component functions and single-index coefficient functions (available from the returned famTEMsel object) can be used to make individualized treatment recommendations (ITRs) for future subjects; see also make_ITR_famTEMsel for such ITRs.

The regularization path for the component functions is computed at a grid of values for the regularization parameter lambda.

## Value

a list of information of the fitted constrained functional additive models including
samTEMsel.obj an object of class samTEMsel, which contains the sequence of the set of fitted component functions implied by the sequence of the regularization parameters lambda; the sparse additive models are fitted over the set of the $p$ functional covariates projected onto the estimated single-index coefficient functions (stored in si.fit) and the set of q scalar covariates; the object samTEMsel. obj includes the residuals of the fitted models and the fitted values for the response variable; see samTEMsel: : samTEMsel for detail of the samTEMsel object.
si.fit the length-p list of the single-index coefficient function estimate objects; each element is a mgcv::gam object; the jth element corresponds to the estimated single-index coefficient function associated with the jth functional covariate.
si.coef. path the length-p list, where the jth element is a (iter-by-k) matrix, with the lth row corresponding to the basis coefficient vector estimate associated with the jth single-index coefficient function at the lth iteration of the fitting procedure.
mean.fn the length-p list of mean functions (averaged across $n$ observations), where the jth element is a n.eval[j]-by- 1 vector of the evaluation of the estimated mean of the jth functional covariate.
n.eval a length-p vector, where its jth element represents the number of evaluation points of the jth functional covariate.
func_norm.record
the iter-by $-(\mathrm{p}+\mathrm{q})$ matrix, with its lth row corresponding to the vector of the estimated ( $\mathrm{p}+\mathrm{q}$ ) component functions' L2 norms at the lth iteration.
func_norm a length $(p+q)$ vector of the estimated $(p+q)$ component functions' $L 2$ norms, at the final iteration.
lambda the sequence of regularization parameters used in the object samTEMsel.obj.
lambda.index an index number, indicating the index of the regularization parameter in lambda used in obtaining the fitted model (including the single-index coefficient functions).
nonzero.index a set of numbers, indicating the indices of estimated nonzero component functions of this particular fit under the regularization parameter index lambda. index.
nonzero. X.index
a set of numbers, indicating the indices of estimated nonzero component functions associated with the p functional covariates, based on this particular fit under the regularization parameter index lambda. index.

## Author(s)

Park, Petkova, Tarpey, Ogden

## See Also

cv.famTEMsel, predict_famTEMsel, plot_famTEMsel, make_ITR_famTEMsel

## Examples

```
p=q=10# p and q are the numbers of functional and scalar pretreatment covariates, respectively.
n.train = 300 # training set sample size
```

```
n.test = 1000 # testing set sample size
n = n.train + n.test
# generate p pretreatment functional covariates X by first seting up functional basis:
n.eval = 50; s = seq(0, 1, length.out = n.eval) # a grid of support points
b1 = sqrt(2)*sin(2*pi*s)
b2 = sqrt(2)*\operatorname{cos}(2*pi*s)
b3 = sqrt(2)*sin(4*pi*s)
b4 = sqrt(2)*cos(4*pi*s)
B = cbind(b1, b2, b3, b4) # a (n.eval-by-4) basis matrix
# randomly generate basis coefficients, and then add measurement noise
X = vector("list", length= p); for(j in 1:p){
    X[[j]] = matrix(rnorm(n*4, 0, 1), n, 4) %*% t(B) +
        matrix(rnorm(n*n.eval, 0, 0.25), n, n.eval) # measurement noise
}
Z = matrix(rnorm(n*q, 0, 1), n, q) # q scalar covariates
A = rbinom(n, 1, 0.5) + 1 # treatment variable taking a value in {1,2} with equal prob.
# X main effect on y; depends on the first 5 covariates
# the effect is generated randomly; randomly generated basis coefficients, scaled to unit L2 norm.
tmp = apply(matrix(rnorm(4*5), 4,5), 2, function(s) s/sqrt(sum(s^2) ))
main.effect = rep(0, n); for(j in 1:5){
    main.effect = main.effect + cos(X[[j]]%*% B%*%tmp[,j]/n.eval) # nonlinear effect (cosine)
}; rm(tmp)
# Z main effect on y; also depends on first 5 covariates
for(k in 1:5){
    main.effect = main.effect + cos(Z[,k])
}
# define (interaction effect) coefficient functions associted with X[[1]] and X[[2]]
beta1 = B %*% c(0.5,0.5,0.5,0.5)
beta2 = B %*% c(0.5,-0.5,0.5,-0.5)
# A-by-X ineraction effect on y; depends only on X[[1]] and X[[2]].
interaction.effect = (A-1.5)*( 2*sin(X[[1]]%*%beta1/n.eval) + 2*sin(X[[2]]%*%beta2/n.eval))
# A-by-Z ineraction effect on y; depends only on Z[,1] and Z[,2].
interaction.effect = interaction.effect + (A-1.5)*(Z[,1] + 2*sin(Z[,2]))
# generate outcome y
noise = rnorm(n, 0, 0.5)
y = main.effect + interaction.effect + noise
var.main <- var(main.effect)
var.interaction <- var(interaction.effect)
var.noise <- var(noise)
SNR <- var.interaction/ (var.main + var.noise)
SNR # "signal-to-noise" ratio
# train/test set splitting
train.index = 1:n.train
y.train = y[train.index]
X.train= X.test = vector("list", p); for(j in 1:p){
    X.train[[j]] = X[[j]][train.index,]
    X.test[[j]] = X[[j]][-train.index,]
}
A.train = A[train.index]
A.test = A[-train.index]
y.train = y[train.index]
```

```
y.test = y[-train.index]
Z.train = Z[train.index,]
Z.test = Z[-train.index,]
# fit a model with some regularization parameter index, say, lambda.index = 10.
# (an optimal regularization parameter can be estimated by running cv.famTEMsel().)
famTEMsel.obj = famTEMsel(y.train, A.train, X.train, Z.train, lambda.index=10)
famTEMsel.obj$func_norm # L2 norm of the estimated component functions of the model
famTEMsel.obj$nonzero.index # set of indices for the component functions estimated as nonzero
# plot the component functions estimated as nonzero and the single-index functions
plot_famTEMsel(famTEMsel.obj, which.index = famTEMsel.obj$nonzero.index)
# make ITRs for subjects with pretreatment characteristics, X.test and Z.test
trt.rule = make_ITR_famTEMsel(famTEMsel.obj, newX = X.test, newZ = Z.test)$trt.rule
head(trt.rule)
# an (IPWE) estimate of the "value" of this particualr treatment rule, trt.rule:
mean(y.test[A.test==trt.rule])
# compare the above value to the following estimated "values" of "naive" treatment rules:
mean(y.test[A.test==1]) # a rule that assigns everyone to A=1
mean(y.test[A.test==2]) # a rule that assigns everyone to A=2
```

make_ITR_famTEMsel make individualized treatment recommendations (ITRs) based on a famTEMsel object

## Description

The function make_ITR_famTEMsel returns individualized treatment decision recommendations for subjects with pretreatment characteristics newX and newZ, given a famTEMsel object, famTEMsel .obj, and an (optimal) regularization parameter index, lambda.index.

## Usage

make_ITR_famTEMsel(famTEMsel.obj, newX = NULL, newZ = NULL, lambda.index = NULL, maximize = TRUE)

## Arguments

famTEMsel.obj a famTEMsel object, containing the fitted constrained functional additive models.
newX a length-p list of new values for the functional-valued covariates X , where the jth element is a (n-by-n.eval[j]) matrix of the observed jth function, at which predictions are to be made; if NULL, X from the training set is used.
newZ a (n-by-q) matrix of new values for the scalar-valued covariates $Z$ at which predictions are to be made; if NULL, Z from the training set is used.
lambda.index an index of the regularization parameter lambda at which predictions are to be made; one can supply lambda. opt. index obtained from the function cv. famTEMsel(); the default is NULL, in which case the predictions are made at the lambda. index used in obtaining famTEMsel.obj.
maximize default is TRUE, assuming a larger value of the outcome is better; if FALSE, a smaller value is assumed to be prefered.

## Value

pred.new a (n-by-L) matrix of predicted values, with each column representing one of the L treatment options.
trt.rule a (n-by-1) vector of the individualized treatment recommendations

## Author(s)

Park, Petkova, Tarpey, Ogden

## See Also

famTEMsel,cv.famTEMsel, predict_famTEMsel

## plot_famTEMsel plot component functions from a famTEMsel object

## Description

Produces plots of the component functions and the single-index coefficient functions from a famTEMsel object.

## Usage

```
plot_famTEMsel(famTEMsel.obj, newX = NULL, newZ = NULL, newA = NULL,
    scatter.plot = TRUE, lambda.index = famTEMsel.obj$lambda.index,
    which.index = famTEMsel.obj$nonzero.index, ylims,
    single.index.plot = TRUE, solution.path = FALSE)
```


## Arguments

famTEMsel.obj a famTEMsel object
newX a ( n by p ) list of new values for the functional covariates X at which predictions are to be made; the jth element of the list corresponds to a n-by-n.eval[j] matrix of the observed jth functional covariates; n.eval[j] represents the number of evaluation points of the jth functional covariates; if NULL, X from the training set is used.
newZ a (n by q) matrix of new values for the scalar covariates Z at which predictions are to be made; if NULL, Z from the training set is used.
newA a (n-by-1) vector of new values for the treatment $A$ at which plots are to be made; the default is NULL, in which case A is taken from the training set.
scatter.plot if TRUE, draw scatter plots of partial residuals versus the covariates; these scatter plots are made based on the training observations; the default is TRUE.
lambda.index an index of the tuning parameter lambda at which plots are to be made; one can supply lambda.opt.index obtained from the function cv.samTEMsel; the default is NULL, in which case plot_samTEMsel utilizes the most non-sparse model.

```
which.index this specifies which component functions are to be plotted; the default is all p
    component functions, i.e., 1:p.
ylims this specifies the vertical range of the plots, e.g., c(-10, 10).
single.index.plot
    if TRUE, draw the plots of the estimated single-index coefficient functions; the
    default is TRUE.
solution.path if TRUE, draw the functional norms of the fitted component functions (based on
    the training set) versus the regularization parameter; the default is FALSE.
```


## Author(s)

Park, Petkova, Tarpey, Ogden

```
See Also
famTEMsel,predict_famTEMsel, cv.famTEMsel
```

predict_famTEMsel famTEMsel prediction function

## Description

predict_famTEMsel makes predictions given a (new) set of functional covariates newX, a (new) set of scalar covariates newZ and a (new) vector of treatment indicators newA based on a constrained functional additive model famTEMsel.obj. Specifically, predict_famTEMsel predicts the responses $y$ based on the (X,Z)-by-A interaction effect (plus the A main effect) portion of the full model that includes the unspecified $X$ main effect term.

## Usage

predict_famTEMsel(famTEMsel.obj, newX = NULL, newZ = NULL, newA $=$ NULL, type $=$ "response", lambda.index $=$ NULL)

## Arguments

famTEMsel.obj a famTEMsel object
newX $\quad a(n$ by $p$ ) list of new values for the functional covariates $X$ at which predictions are to be made; the jth element of the list corresponds to a n-by-n.eval[j] matrix of the observed jth functional covariates; n.eval[j] represents the number of evaluation points of the jth functional covariates; if NULL, X from the training set is used.
newZ a (n by q) matrix of new values for the scalar covariates Z at which predictions are to be made; if NULL, Z from the training set is used.
newA a (n by 1) vector of new values for the treatment A at which predictions are to be made; if NULL, A from the training set is used.
type the type of prediction required; the default "response" gives the predicted responses y based on the whole model; the alternative "terms" gives the componentwise predicted responses from each of the p components (and plus the treatmentspecific intercepts) of the model.
lambda. index an index of the tuning parameter lambda at which predictions are to be made; one can supply lambda. opt.index obtained from the function cv. samTEMsel; the default is NULL, in which case the predictions based on the most non-sparse model is returned.

## Value

predicted a(n-by-length(lambda.index)) matrix of predicted values; a (n-by-length(lambda.index)*(p+qmatrix of predicted values if type = "terms", where the last column corresponds to the (treatment-specific) intercept.

U a n-by- $(\mathrm{p}+\mathrm{q})$ matrix of the index variables; the first p columns correspond to the 1-D projections of the p functional covariates and the last q columns correspond to the q scalar covariates.

## Author(s)

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See Also
famTEMsel,cv.famTEMsel, plot_famTEMsel

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